

Supplementary Materials for

A thermodynamic model for predicting carbon dioxide solubility in aqueous sodium chloride solutions using an association equation of state

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Section 1: CPA EoS

The CPA EoS is used for the vapor phase as follows:

$$P = \frac{RT}{v-b} - \frac{\alpha(T)}{v(v+b)} - \frac{1}{2} \frac{RT}{v} \left(1 + \frac{1}{v} \frac{\partial \ln g}{\partial (1/v)} \right) \sum_{i=1}^n y_i \sum_{A_i} (1 - X_{A_i}) \quad (S1)$$

where v is molar volume, $\text{cm}^3 \cdot \text{mol}^{-1}$; $\alpha(T)$ and b are respectively the energy parameter and co-volume of CPA EoS; A and B stand for the bonding sites; y_i is the molar fraction of given component i ; X_{A_i} is the molar fraction of i molecules not bonded at site A; g is the radial distribution function.

The energy parameter is given by:

$$\alpha(T) = a_0 \left[1 + c_1 (1 - \sqrt{T_r}) \right]^2 \quad (S2)$$

where a_0 and c_1 are parameters of CPA EoS; T_c is the critical temperature, K; T_r is equal to T/T_c .

The X_{A_i} in the association term can be calculated by

$$X_{A_i} = \left(1 + \left(\frac{1}{v} \right) \sum_j y_j \sum_{B_j} X_{B_j} \Delta^{A_i B_j} \right)^{-1} \quad (S3)$$

$$\Delta^{A_i B_j} = g(v) \left[\exp \left(\frac{\varepsilon^{A_i B_j}}{RT} \right) - 1 \right] b_{ij} \beta^{A_i B_j} \quad (S4)$$

where $\varepsilon^{A_i B_j}$ is association energy; $\beta^{A_i B_j}$ is interaction volume; $\Delta^{A_i B_j}$ is association strength.

The radial distribution function is as follows:

$$g(v) = \frac{1}{(1 - 1.9\eta)} \quad (S5)$$

$$\eta = \frac{1}{4v} b \quad (S6)$$

where η is reduced fluid density.

Table S1 includes the parameters of the CPA EoS of pure CO_2 and H_2O .

Table S1 Parameters of CPA EoS of pure CO₂ and H₂O.

Fluid	Association scheme	a_0 (cm ² ·MPa·mol ⁻²)	b (cm ³ ·mol ⁻¹)	c_1	ε (cm·MPa·mol ⁻¹)	β
CO ₂	Inert	350790	27.2	0.7602	-	-
H ₂ O	4C	122770	14.5	0.6736	16655	0.0692

Section 2: Derivatives of a_{CO_2} and $a_{\text{H}_2\text{O}}$

The derivatives of a_{CO_2} and $a_{\text{H}_2\text{O}}$ with respect to m_{CO_2} are Eqs. (S7) and (S8).

$$\frac{\partial a_{\text{CO}_2}}{\partial m_{\text{CO}_2}} = \gamma_{\text{CO}_2} + \gamma_{\text{CO}_2} m_{\text{CO}_2} \left[2\lambda_{nn} + 6m_{\text{CO}_2} \mu_{nnn} + 6m_{\text{NaCl}} (\mu_{nnc} + \mu_{nna}) \right] \quad (\text{S7})$$

$$\begin{aligned} \frac{\partial a_{\text{H}_2\text{O}}}{\partial m_{\text{CO}_2}} = & -\frac{a_{\text{H}_2\text{O}} M_{\text{H}_2\text{O}}}{1000} \left\{ 1 + 2 \left[m_{\text{CO}_2} \lambda_{nn} + 3m_{\text{CO}_2}^2 \mu_{nnn} + m_{\text{NaCl}} (\lambda_{nc} + \lambda_{na}) \right. \right. \\ & \left. \left. + 6m_{\text{CO}_2} m_{\text{NaCl}} (\mu_{nnc} + \mu_{nna}) + m_{\text{NaCl}}^2 \xi_{nca} \right] \right\} \end{aligned} \quad (\text{S8})$$

The parameters of λ_{nn} and μ_{nnn} are adopted from Zhao et al. (2015^[5]) as follows:

$$\lambda_{nn} = -0.16662 + 4.9482 \times 10^{-4} T - 5.1643 \times 10^{-7} T^2 \quad (\text{S9})$$

$$\mu_{nnn} = -0.089196 - 2.8829 \times 10^{-4} T + 2.3197 \times 10^{-7} T^2 \quad (\text{S10})$$

The parameters of λ_{nc} , λ_{na} , μ_{nna} , and μ_{nnc} are reported by Akinfiev and Diamond (2010)^[82] as follows:

$$\begin{aligned} (\lambda_{nc} + \lambda_{na}) = & 0.057123 + \frac{2.6994}{T - 228} \\ & + \frac{0.045635}{2I} \left[1 - (1 + 2\sqrt{I}) \exp(-2\sqrt{I}) \right] \end{aligned} \quad (\text{S11})$$

$$(\mu_{nnc} + \mu_{nna}) = -5.76 \times 10^{-4} \quad (\text{S12})$$